1. PHYSICAL CONSTANTS

Table 1.1. Reviewed 1998 by B.N. Taylor (NIST). Based mainly on the "1986 Adjustment of the Fundamental Physical Constants" by E.R. Cohen and B.N. Taylor, Rev. Mod. Phys. **59**, 1121 (1987). The last group of constants (beginning with the Fermi coupling constant) comes from the Particle Data Group. The figures in parentheses after the values give the 1-standarddeviation uncertainties in the last digits; the corresponding uncertainties in parts per million (ppm) are given in the last column. This set of constants (aside from the last group) is recommended for international use by CODATA (the Committee on Data for Science and Technology).

Since the 1986 adjustment, new experiments have yielded improved values for a number of constants, including the Rydberg constant R_{∞} , the Planck constant h, the finestructure constant α , and the molar gas constant R, and hence also for constants directly derived from these, such as the Boltzmann constant k and Stefan-Boltzmann constant σ . The new results and their impact on the 1986 recommended values are discussed extensively in "Recommended Values of the Fundamental Physical Constants: A Status Report," B.N. Taylor and E.R. Cohen, J. Res. Natl. Inst. Stand. Technol. 95, 497 (1990); see also E.R. Cohen and B.N. Taylor, "The Fundamental Physical Constants," Phys. Today, August 1997 Part 2, BG7. In general, the new results give uncertainties for the affected constants that are 5 to 7 times smaller than the 1986 uncertainties, but the changes in the values themselves are smaller than twice the 1986 uncertainties. Because the output values of a least-squares adjustment are correlated. the new results cannot readily be incorporated with the 1986 values. Until the next complete adjustment of the constants (expected by the end of 1998), the 1986 CODATA set, given (in part) below, remains the set of choice. The full 1986 set (to be replaced by the new set, when available) may be found at http://physics.nist.gov/cuu.

2 1. Physical constants

c speed of light in vacuum

Value: $299 792 458 \text{ m s}^{-1}$ Uncert. (ppm): exact^*

* The meter is the length of the path traveled by light in vacuum during a time interval of 1/299 792 458 of a second.

h Planck constant

Value: $6.626\ 075\ 5(40) \times 10^{-34}\ J\ s$

Uncert. (ppm): 0.60

$\hbar \equiv h/2\pi$ Planck constant, reduced

Value: $1.054\ 572\ 66(63) \times 10^{-34}\ \mathrm{J\ s}$

Uncert. (ppm): 0.60

Value: $= 6.582 \ 122 \ 0(20) \times 10^{-22} \ \text{MeV s}$

Uncert. (ppm): 0.30

e electron charge magnitude

Value: $1.602\ 177\ 33(49) \times 10^{-19}\ C = 4.803\ 206\ 8(15) \times 10^{-10}\ esu$

Uncert. (ppm): 0.30, 0.30

$\hbar c$ conversion constant

Value: 197.327 053(59) MeV fm

Uncert. (ppm): 0.30

$(\hbar c)^2$ conversion constant

Value: $0.389\ 379\ 66(23)\ \text{GeV}^2\ \text{mbarn}$

Uncert. (ppm): 0.59

m_e electron mass

Value: $0.510\,999\,06(15)\,\text{MeV}/c^2 = 9.109\,389\,7(54)\times10^{-31}\,\text{kg}$

Uncert. (ppm): 0.30, 0.59

m_p proton mass

Value: $938.272 \ 31(28) \ \text{MeV}/c^2 = 1.672 \ 623 \ 1(10) \times 10^{-27} \ \text{kg}$

Uncert. (ppm): 0.30, 0.59

Value: $= 1.007 \ 276 \ 470(12) \ u = 1836.152 \ 701(37) \ m_e$

Uncert. (ppm):0.012, 0.020

m_d deuteron mass

Value: $1875.613 \ 39(57) \ \text{MeV}/c^2$

Uncert. (ppm): 0.30

Rydberg energy

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(mass ^{12}C atom)/12 = (1 g)/(N_A mol) unified atomic mass unit (u) Value: 931.494 32(28) MeV/c^2 = 1.660 540 2(10)×10<sup>-27</sup> kg
   Uncert. (ppm): 0.30, 0.59
\epsilon_0 \quad \epsilon_0 \mu_0 = 1/c^2 permittivity of free space Value: 8.854 187 817 . . . . \times 10^{-12}~\mathrm{F~m^{-1}}
   Uncert. (ppm): exact
\mu_0 \quad \epsilon_0 \mu_0 = 1/c^2 permeability of free space Value: 4\pi \times 10^{-7} \ \mathrm{N} \ \mathrm{A}^{-2} = 12.566\ 370\ 614 \ldots \times 10^{-7} \ \mathrm{N} \ \mathrm{A}^{-2}
   Uncert. (ppm): exact
\alpha = e^2/4\pi\epsilon_0\hbar c fine-structure constant
   Value: 1/137.0359895(61)^{\dagger}
  Uncert. (ppm): 0.045
<sup>†</sup> At Q^2 = 0. At Q^2 \approx m_W^2 the value is approximately 1/128.
r_e = e^2/4\pi\epsilon_0 m_e c^2
                                         classical electron radius
  Value: 2.81794092(38) \times 10^{-15} \text{ m}
   Uncert. (ppm): 0.13
\lambda_e = \hbar/m_e c = r_e \alpha^{-1} electron Compton wavelength
   Value: 3.861\ 593\ 23(35) \times 10^{-13}\ m
   Uncert. (ppm): 0.089
a_{\infty} = 4\pi\epsilon_0 \hbar^2/m_e e^2 = r_e \alpha^{-2}
                                                       Bohr radius (m_{\text{nucleus}} = \infty)
  Value: 0.529\ 177\ 249(24) \times 10^{-10}\ m
   Uncert. (ppm): 0.045
hc/e
                      wavelength of 1 \text{ eV}/c particle
   Value: 1.239\ 842\ 44(37)\times10^{-6}\ m
  Uncert. (ppm): 0.30
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Thomson cross section

 $hcR_{\infty} = m_e e^4 / 2(4\pi\epsilon_0)^2 \hbar^2 = m_e c^2 \alpha^2 / 2$

Value: 13.605 698 1(40) eV

Value: 0.665 246 16(18) barn

Uncert. (ppm): 0.30

Uncert. (ppm): 0.27

 $\sigma_T = 8\pi r_e^2 / 3$

4 1. Physical constants

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\mu_B = e\hbar/2m_e
                               Bohr magneton
  Value: 5.788\ 382\ 63(52) \times 10^{-11}\ \mathrm{MeV}\ \mathrm{T}^{-1}
  Uncert. (ppm): 0.089
\mu_N = e\hbar/2m_p
                               nuclear magneton
  Value: 3.15245166(28)\times10^{-14} \text{ MeV T}^{-1}
  Uncert. (ppm): 0.089
\omega_{\rm cycl}^e/B = e/m_e
                                  electron cyclotron freq./field
  Value: 1.758\ 819\ 62(53) \times 10^{11}\ \mathrm{rad\ s^{-1}\ T^{-1}}
  Uncert. (ppm): 0.30
\omega_{\mathrm{cvcl}}^p/B = e/m_p
                                  proton cyclotron freq./field
  Value: 9.578~830~9(29)\times10^7~{\rm rad~s^{-1}~T^{-1}}
  Uncert. (ppm): 0.30
                  gravitational constant<sup>‡</sup>
G_N
  Value: 6.672\ 59(85) \times 10^{-11}\ \mathrm{m^3\ kg^{-1}\ s^{-2}}
  Uncert. (ppm): 128
  Value: = 6.707 \ 11(86) \times 10^{-39} \ \hbar c \ (\text{GeV}/c^2)^{-2}
  Uncert. (ppm): 128
<sup>‡</sup> Absolute lab measurements of G_N were performed only on scales of 10^{-1\pm1} m.
               standard grav. accel., sea level
  Value: 9.806 65 \text{ m s}^{-2}
  Uncert. (ppm): exact
                  Avogadro constant
N_A
  Value: 6.022\ 136\ 7(36) \times 10^{23}\ \text{mol}^{-1}
  Uncert. (ppm): 0.59
                Boltzmann constant
  Value: 1.380 658(12) \times 10^{-23} \text{ J K}^{-1}
  Uncert. (ppm): 8.5
  Value: = 8.617 \ 385(73) \times 10^{-5} \ eV \ K^{-1}
  Uncert. (ppm): 8.4
N_A k(273.15 \text{ K})/(101 325 \text{ Pa})
                                                  molar volume, ideal gas at STP
  Value: 22.414\ 10(19) \times 10^{-3}\ \text{m}^3\ \text{mol}^{-1}
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Uncert. (ppm): 8.4

Wien displacement law constant $b = \lambda_{\text{max}} T$

Value: $2.897756(24) \times 10^{-3} \text{ m K}$

Uncert. (ppm): 8.4

 $\sigma = \pi^2 k^4 / 60 \hbar^3 c^2$ Stefan-Boltzmann constant

Value: $5.670 \, 51(19) \times 10^{-8} \, \text{W m}^{-2} \, \text{K}^{-4}$

Uncert. (ppm): 34

 $F_F/(\hbar c)^3$ Fermi coupling constant** Value: $1.166~39(1)\times10^{-5}~{\rm GeV}^{-2}$ $G_F/(\hbar c)^3$

Uncert. (ppm): 9

** See discussion in Sec. 10 "Electroweak model and constraints on new physics."

 $\sin^2 \widehat{\theta}(M_Z)$ (MS) weak mixing angle

Value: 0.23124(24) Uncert. (ppm): 1000

 W^\pm boson mass m_W

Value: $80.41(10) \text{ GeV}/c^2$ Uncert. (ppm): 1200

 Z^0 boson mass m_Z

Value: $91.187(7) \text{ GeV}/c^2$

Uncert. (ppm): 77

 $\alpha_s(m_Z)$ strong coupling constant

Value: 0.119(2)

Uncert. (ppm): 17000

6 1. Physical constants

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\begin{split} \pi &= 3.141\ 592\ 653\ 589\ 793\ 238\\ e &= 2.718\ 281\ 828\ 459\ 045\ 235\\ \gamma &= 0.577\ 215\ 664\ 901\ 532\ 861 \end{split}
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1 atmosphere $\equiv 760 \text{ torr} \equiv 101 325 \text{ Pa}$

$$1 \text{ in} \equiv 0.0254 \text{ m}$$

$$1 \text{ Å} \equiv 10^{-10} \text{ m}$$

$$1 \text{ barn} \equiv 10^{-28} \text{ m}^2$$

$$1 \text{ G} \equiv 10^{-4} \text{ T}$$

$$1 \text{ dyne} \equiv 10^{-5} \text{ N}$$

$$1 \text{ erg} \equiv 10^{-7} \text{ J}$$

$$1 \text{ eV} = 1.602 \text{ 177 } 33(49) \times 10^{-19} \text{ J}$$

$$1 \text{ eV}/c^2 = 1.782 \text{ 662 } 70(54) \times 10^{-36} \text{ kg}$$

$$2.997 \text{ 924 } 58 \times 10^9 \text{ esu} = 1 \text{ C}$$

$$kT \text{ at } 300 \text{ K} = [38.681 \text{ } 49(33)]^{-1} \text{ eV}$$

$$0 \text{ °C} \equiv 273.15 \text{ K}$$